# Energy-Efficient Multi-Stream Carrier Aggregation for Heterogeneous Networks in 5G Cellular Systems

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Abstract-Multi-stream carrier aggregation (MSCA) has been recently proposed as a mechanism to increase the amount of bandwidth available to users for heterogeneous networks (HetNets) in 5G cellular systems. Previous studies have focused only on maximizing the network capacity and fairness, without considering the energy efficiency of the MSCA. In this paper, the use of MSCA to minimize the energy consumption in a multilayer HetNet is studied. The convexity of the energy minimization problem is examined, leading to the need of a quasiconvex relaxation. With this approximation, an algorithm (BIMEM) is designed to solve the energy minimization problem and obtain an optimum cell-association policy. Since the operators are generally interested in a balance between the energy minimization and capacity maximization, such multi-objective optimization is needed, and we studied it in this paper. The two aforementioned conflicting objectives can be jointly analyzed and solved through scalarization, even though the energy minimization has a quasiconvex objective function, and not a convex one. Performance evaluation is provided to identify the achievable energy savings of our proposed algorithm and to characterize the trade-offs between the energy minimization and capacity maximization in a multi-layer HetNet in 5G systems that support MSCA.

*Index Terms*—Heterogeneous networks, energy saving, cellular networks, cell-association, multi-stream, carrier aggregation.

## I. INTRODUCTION

One of the most effective methods to improve the performance in cellular networks is to increase the amount of utilized bandwidth. Therefore, to meet the requirements of IMT-Advanced<sup>1</sup> [1], as well as those of the operators, the Long Term Evolution (LTE) Advanced (LTE-Advanced) considers the use of bandwidths of up to 100MHz in several frequency bands [2]. These bands are set by the International Telecommunication Union (ITU) and include the following [3]: 450-470MHz, 698-960MHz, 1710-2025MHz, 2110-2200MHz, 2300-2400MHz, 2500-2690MHz, 3400-3600MHz. For the fifth generation (5G) cellular systems, the use of even higher and wider frequency bands, such as millimeter wave ones, is a key enabling technology [4] [5]. LTE-Advanced tries to exploit as much as possible the flexibility of supporting multiple frequency bands through the use of carrier aggregation [6] [7].

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<sup>1</sup>IMT-Advanced stands for international mobile telecommunicationsadvanced. Carrier aggregation (CA) consists of grouping several component carriers (CC) to achieve wider transmission bandwidths. An LTE-Advanced device can aggregate up to five CCs, each of up to 20 MHz. With the largest configuration, this implies a total bandwidth of 100MHz. To support backward compatibility with LTE user equipment (UE), each of the CCs shall be configured as a typical LTE carrier. Therefore, any of the CCs used for CA should also be accessible to LTE UEs. Nevertheless, mechanisms, such as barring [8], already exist to prevent LTE UEs from camping on specific CCs. This way, operators have the flexibility of adjusting the characteristics of the CCs to support a mixture of LTE and LTE-Advanced devices.

To obtain the most benefit from CA, each base station (BS) should support the maximum number of CCs<sup>2</sup>. Nevertheless, in current 4G and even more so in future 5G systems, cellular networks are composed of a combination of small cells that provide enhanced coverage in targeted areas and macrocells that provide basic coverage, creating a HetNet [9] [10]. In most HetNet scenarios, not all BSs support the maximum CA configuration. This is mainly due to the hardware limitations, which require costly upgrades. Multi-stream CA (MSCA), also known as multi-flow CA, has been recently proposed as an alternative method to address this problem [11] [12] [13]. In MSCA, a UE is able to aggregate CCs belonging to multiple BSs, allowing it to achieve the maximum CA configuration, even if no BS can provide such configuration by itself.

In non-MSCA networks, the existing literature has looked at multiple ways of reducing the network energy consumption. In [14], the use of lean carriers with reduced signaling overhead is proposed. By reducing the signaling overhead, the BS can go into micro-sleep more frequently. The concept of adjusting the cell-association policies and, therefore, the load across BSs has also been proposed separately for energy minimization [15] and user fairness [16] [17] [18]. Furthermore, cooperation among BSs has been utilized to minimize the energy consumption by coordinating the scheduling and power control mechanisms [19] [20] and the on-off policies [21] [22]. Compared to the literature on non-MSCA, existing work on MSCA-enabled networks has focused on maximizing the network capacity [23] [24], achieving a target SINR [25] [26], and the analysis of the impact of biasing and the selection of frequency bands [27] [28]. However, even though reducing the energy consumption is a key design factor for 5G cellular systems [10] [29], almost no work has been done on analyzing

<sup>&</sup>lt;sup>2</sup>The current version of the standard specifies the maximum configuration to be five CCs.



Fig. 1. MSCA in a HetNet.

energy-efficient methods of exploiting MSCA [30].

The focus of our work is designing new methods of exploiting MSCA to improve the energy efficiency in multilayer HetNets for current 4G and future 5G cellular systems. In particular, we show that the energy minimization problem in MSCA-enabled networks is a non-convex optimization. Nevertheless, such problem can be approximated through a generalized linear-fractional program. Using this approximation, we develop a simple algorithm to solve such problem by applying a bisection method that solves a convex feasibility problem at each step, until a precision tolerance is met. Since the operators are typically interested not only in minimizing the energy consumption, but also in maximizing the network capacity, we analyze these problems jointly as a multi-objective optimization. Based on the analysis done for the energy minimization problem, we provide a solution for the multi-objective one, according to the priority assigned by the operators to each objective. Moreover, we show that an explicit analytical expression for the UE-to-CC association policy can be obtained without the need of solving the multi-objective optimization problem.

The rest of this paper is organized as follows. We present the network architecture and BS energy model in Sections II-A and II-B, respectively. In Section III, we develop the energyand capacity-aware mechanisms of load balancing that exploit the use of MSCA. In particular, in Section III-A, we focus on the single objective of minimizing the network energy consumption. Then, the energy minimization and capacity maximization are jointly analyzed in Section III-B. Simulation results showing the performance of our load-balancing mechanisms are presented in Section IV. Finally, the conclusions are presented in Section V.

## **II. SYSTEM MODEL**

## A. Network Architecture

An example of a network where a UE and the BSs support MSCA is depicted in Figure 1. From Figure 1, we observe that the UE applies MSCA by connecting to three CCs that belong to BSs of different layers. This behavior follows from the fact that the BSs in the same layer are typically assigned the same frequency bands. Therefore, if a UE were to connect to multiple BSs of the same layer, it would have to utilize advanced intercell interference cancellation (ICIC) techniques to recover the signal from each BS [31] [32] [33]. While not impossible, such functionality is not within the scope of MSCA; rather, it is included in cooperative multipoint transmission and reception (CoMP) [34] [35]. CoMP requires not only advanced ICIC at the UE, but also a significant amount of coordination between the BSs, so that their transmission scheme is suitable for the application of advanced ICIC at the UE [36] [37] [38]. Compared to CoMP, the overhead associated with MSCA is significantly smaller since there is no need to coordinate or synchronize among the CCs used for MSCA how the physical resources are utilized.

For the purpose of MSCA, we stipulate that any pair of BSs that belong to different layers will utilize CCs that operate on different frequency bands. On the other hand, BSs that belong to the same layer may utilize CCs that operate on the same frequency bands. We consider that the network serves a set of users  $\mathcal{U}$  and that each user can generate sessions that have different quality of service (QoS) requirements  $q \in \mathcal{Q}$ . These are defined in terms of bit rates, to capture the non-linear relationship between bit rate and power. We also consider that each UE  $u_i$  has a set  $\Gamma_i$  of active CCs. A given  $\Gamma_i$  contains at most one CC for every frequency band. Among all the CCs that belong to the same frequency band, a given UE  $u_i$  will add to its  $\Gamma_i$  the CC towards which the value of pathloss plus shadowing is the smallest. While other methods of selecting the set  $\Gamma_i$  could be explored, they are out of the scope of this article and will be explored in future work. In addition, we consider that each UE is capable of partitioning every session across all of its active CCs. Such assumption is justified by the fact that, if we were to consider that a session can only be served through a single CC, the overall problem would be reduced to a flow-to-CC association problem, which is equivalent to the traditional UE-to-CC cellassociation problem when no MSCA is considered. Moreover, we consider that the processes of partitioning the traffic at the UE and recombining such traffic at the network introduce a negligible bit rate overhead to the total bit rate required to satisfy a session. Furthermore, the analysis is done considering single-antenna systems; the extension to multi-antenna systems will be explored in future work. In terms of the channel, we consider path loss, shadowing and its auto-correlation effects, and non-selective block fading. From the network perspective, we consider the load of a BS to be represented by the total bit rate it provides to the UEs that it serves. Thus, from now on we will use the terms bit rate and load interchangeably. Our definition of network load represents the input that the network needs to support, regardless of how the network utilizes its own resources to handle the input - which is the definition of load used in some existing work [39]. As a result, with our definition, the load metric becomes a function of the traffic, i.e., the input, and not of what our algorithm does with the network resources.

#### B. Base Station Energy Model

In terms of the energy consumption of the BS, we consider that each BS b has a set  $S_b$  of CCs. From now on, we will utilize the notation  $CC_{j,k}$  to denote CC k of BS j. We consider the energy consumption model of an active  $CC_{j,k}$  during a time interval  $\Delta t$  to be

$$\hat{E}_{\text{total}}(\text{CC}_{j,k}) = \Delta t \left[ \hat{P}_{\text{on,min}}(\text{CC}_{j,k}) + \hat{P}_{\text{on,dyn}}(\text{CC}_{j,k}) \right], \quad (1)$$

where  $E_{\text{total}}(\text{CC}_{j,k})$  represents the total energy consumption of  $\text{CC}_{j,k}$ ,  $\hat{P}_{\text{on,min}}(\text{CC}_{j,k})$  represents the amount of power consumed regardless of the traffic handled by  $\text{CC}_{j,k}$ , and  $\hat{P}_{\text{on,dyn}}(\text{CC}_{j,k})$  represents the dynamic power consumption of  $\text{CC}_{j,k}$ , which varies with the traffic dynamics. Since  $\hat{P}_{\text{on,min}}(\text{CC}_{j,k})$  is constant with respect to the traffic handled by a CC, it can be excluded from the rest of the analysis. We consider that  $\hat{P}_{\text{on,dyn}}(\text{CC}_{j,k})$  is a linear function of the RF output power required to satisfy the QoS requirements requested by the UEs connected to that CC, as generally done in the literature [40] [41] [42]. Thus, we have that

$$\hat{P}_{\text{on,dyn}}(\text{CC}_{j,k}) = w_{j,k} \sum_{i} P_{i,j,k}, \qquad (2)$$

where  $P_{i,j,k}$  represents the amount of RF output power required by  $CC_{j,k}$  to satisfy the QoS requested by UE *i* and  $w_{j,k}$  is a constant unique for every  $CC_{j,k}$ . The value of not only  $w_{j,k}$ , but also  $\hat{P}_{on,min}(CC_{j,k})$ , depends on the internal components associated with the operation of the CC and their interconnection [43] [44].

## III. ENERGY- AND CAPACITY-AWARE LOAD BALANCING

In a HetNet, the macrocells transmit at a much higher power than the small cells. Thus, regions will exist where a UE will be relatively close to a small cell, but the SINR of a macrocell will still be higher. Therefore, an association policy based on the CC that provides the maximum SINR, i.e., a max-SINR policy, tends to favor the association towards the macrocells over small cells in the aforementioned regions. As a result, a UE close to a small cell may still connect to a macrocell even if

- communicating with the macrocell requires more energy, in uplink or downlink, than communicating with the small cell or
- the macrocell is overloaded, and the small cell resources are being underutilized. Such situation may cause the user QoS requirements to not be satisfied by the macrocell, even though the small cell could have done so.

Moreover, even if a user is capable of following a cellassociation policy different from the max-SINR one, the fact that it can only connect to a single BS means that

- no single cell may have enough capacity to satisfy the downlink and uplink QoS requirements or
- a user may connect to a cell that can satisfy the downlink or uplink QoS requirements, but not both or
- the non-linear relationship between the minimum power received and bit rate would require a disproportional amount of power to satisfy the QoS requirements.

Thus, MSCA can address the aforementioned issues, given that we design mechanisms to balance the load across small cells and macrocells while accounting for the energy consumption and the capacity of each one. The design of such mechanisms for the downlink is the focus of this work. The uplink could be analyzed by following a similar approach, assuming that an accurate model for the UE total energy consumption is available. For UE *i* and  $CC_{j,k}$ , the maximum spectral efficiency  $\theta_{i,j,k}$  of the communication link is a logarithmic function of the SINR:

$$\theta_{i,j,k} = \beta \log_2 \left( 1 + \underbrace{h_{i,j,k} \frac{P_{i,j,k}}{\eta_{i,j,k}}}_{\text{SINR}} \right), \tag{3}$$

where  $P_{i,j,k}$  is the RF output power used by  $CC_{j,k}$  on the resources assigned to UE i,  $h_{i,j,k}$  is the channel gain between UE i and  $CC_{j,k}$ ,  $\eta_{i,j,k}$  represents the noise plus interference experienced by UE *i* when connected to  $CC_{i,k}$ , and  $0 < \beta < 1$  is an attenuation factor that accounts for implementation losses and can be chosen to represent different modem implementations and link conditions [45]. The factor  $h_{i,j,k}$  includes the path loss, fading, and shadowing effects. By considering a large time scale for the association between a user and a CC, the short-term channel dynamics, such as fast fading, can be averaged out, allowing us to consider the SINR and the spectral efficiency as constants during the association duration. For the factor  $\eta_{i,j,k}$ , we consider that there is no intra-cell interference and, to make the formulation tractable, that the expected inter-cell interference within a given layer is known or managed through existing techniques, such as intercell interference coordination.

Even though the maximum spectral efficiency  $\theta_{i,j,k}$  is a good metric for the quality of the channel between user *i* and  $CC_{j,k}$ , the overall bit rate is the metric of interest when determining if the QoS is satisfied. The bit rate achieved over the aforementioned channel depends not only on  $\theta_{i,j,k}$ , but also on the amount of resources assigned to such channel by the BS. Particularly, for user *i*,  $CC_{j,k}$  with bandwidth  $\rho_{j,k}$ , the maximum bit rate  $\tilde{\theta}_{i,j,k}$  over a channel that has a maximum spectral efficiency  $\theta_{i,j,k}$  is

$$\theta_{i,j,k} = \rho_{j,k} y_{i,j,k} \theta_{i,j,k}$$
$$= \rho_{j,k} y_{i,j,k} \beta \log_2 \left( 1 + h_{i,j,k} \frac{P_{i,j,k}}{\eta_{i,j,k}} \right), \qquad (4)$$

where the factor  $0 \leq y_{i,j,k} \leq 1$  represents the fraction of resources reserved for user *i* by  $CC_{j,k}$ , and  $\theta_{i,j,k}$  is obtained from Eq. (3). By considering that the resource allocation is performed within the coherence time of the channel, the latter can be considered static during every allocation period. Such assumption is valid for low-mobility scenarios.

Typically,  $y_{i,j,k} < 1$  since the BS serves more than one user; therefore, it must allocate the limited resources among those users. As a result, the achievable rate of a user depends not only on the channel quality towards a particular CC, but also on the number of other users associated with such CC and the resource allocation policy followed. The latter depends directly on how much bit rate, i.e., load, each UE requests from each CC.

In Section III-A, we focus on finding an optimal loadbalancing and cell-association policy that minimizes the energy consumption of the network. Then, in Section III-B, we utilize the results from Section III-A to develop an optimal load-balancing and cell-association policy capable of addressing the conflicting objectives of minimizing the network energy consumption and maximizing its capacity.

## A. Load Balancing for Energy Minimization

Based on the QoS requirements of all the sessions that a user *i* needs to support, a total bit rate  $r_i$  can be computed for such user. By using MSCA,  $r_i$  can be split across all the CCs to which the UE is capable of connecting. If UE *i* requests a fraction  $0 \le \xi_{i,j,k} \le 1$  of  $r_i$  to  $CC_{j,k}$ , then the following relationship must hold:

$$\xi_{i,j,k} r_i \leq \bar{\theta}_{i,j,k}$$
$$= \rho_{j,k} y_{i,j,k} \beta \log_2 \left( 1 + h_{i,j,k} \frac{P_{i,j,k}}{\eta_{i,j,k}} \right), \qquad (5)$$

where  $\hat{\theta}_{i,j,k}$  is obtained from Eq. (4). The above expression conveys that the amount of bit rate requested by any UE to any CC should not exceed the capacity of the channel between them for a given amount of bandwidth and power allocated to the user. Typically, the above inequality can be treated as an equality, since there is no benefit to the user or BS to have an underutilized channel. Assuming that  $y_{i,j,k} > 0$ , i.e., that  $CC_{j,k}$  is assigning a non-zero amount of bandwidth to user *i*, the amount of output RF power at the antenna of  $CC_{j,k}$  for user *i* can be obtained as follows,

$$P_{i,j,k} = \left[ \exp\left(\frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln\left(2\right)\right) - 1 \right] \frac{\eta_{i,j,k}}{h_{i,j,k}}$$
$$= \frac{\eta_{i,j,k}}{h_{i,j,k}} \exp\left(\frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln\left(2\right)\right) - \frac{\eta_{i,j,k}}{h_{i,j,k}}.$$
 (6)

As discussed in Section II-B, the total dynamic power  $P_{\text{on,dyn}}$  consumed by  $CC_{j,k}$  to output the RF power required to satisfy the QoS requirements of the UEs is a linear function of  $P_{i,j,k}, \forall i, j, k$ :

$$\hat{P}_{\text{on,dyn}}(\text{CC}_{j,k}) = w_{j,k} \sum_{i} P_{i,j,k}$$

$$= w_{j,k} \sum_{i} \frac{\eta_{i,j,k}}{h_{i,j,k}} \exp\left(\frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln\left(2\right)\right)$$

$$- w_{j,k} \sum_{i} \frac{\eta_{i,j,k}}{h_{i,j,k}}.$$
(7)

Based on the expression above, the network energy minimization problem can be described as

minimize 
$$\sum_{j} \sum_{k} \hat{P}_{\text{on,dyn}}(\text{CC}_{j,k}),$$
 (8a)

subject to

$$\sum_{j} \sum_{k} \xi_{i,j,k} = 1, \qquad \forall i, \qquad (8b)$$

$$\sum_{i} y_{i,j,k} \le 1, \qquad \qquad \forall j,k, \qquad (8c)$$

$$\xi_{i,j,k} \ge 0,$$
  $\forall i, j, k,$  (8d)

$$y_{i,j,k} \ge 0, \qquad \forall i, j, k, \qquad (8e)$$
$$r_i \xi_{i,j,k} - \rho_{j,k} \theta_{\max} y_{i,j,k} < 0, \quad \forall i, j, k, \qquad (8f)$$

$$\begin{aligned} & \langle i,j,k \rangle & \langle j,j,k \rangle & = 0; \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j \rangle \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j \rangle \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j \rangle \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j \rangle \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j \rangle \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j \rangle \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle \\ & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle & \langle i,j,k \rangle \\ & \langle i,j,k \rangle \\ & \langle i,j,k \rangle \\ & \langle i,j,k \rangle & \langle i,j,k$$

$$y_{i,j,k} = 0; \qquad \qquad \forall i, j, k, CC_{j,k} \notin \Gamma_i$$

where  $\theta_{max}$  denotes the maximum spectral efficiency supported by the network<sup>3</sup>. Constraint (8b) indicates that the UE total QoS requirement  $r_i$  must be satisfied with equality. Constraint (8c) indicates that  $CC_{i,k}$  cannot allocate more bandwidth than it has available. Constraints (8d) and (8e) indicate that the allocation variables  $\xi_{i,j,k}$  and  $y_{i,j,k}$  are nonnegative. Constraint (8f) indicates that every channel should operate within the maximum spectral efficiency supported by the network. Constraints (8g) and (8h) indicate that a UE i can associate only with the CCs that belong to its active set  $\Gamma_i$  of CCs. All the constraints in the optimization problem (8) are linear expressions. Also, note that in addition to the intrinsic parameters associated with the CCs, the total QoS requirement of each UE and the SINR between the UEs and each BS CC would be required as inputs to solve the optimization problem (8).

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The optimization problem (8) is equivalent to

minimize 
$$\sum_{i,j,k} w_{j,k} \frac{\eta_{i,j,k}}{h_{i,j,k}} \exp\left(\frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln\left(2\right)\right), \quad (9a)$$

where the optimization variables are all the  $\xi_{i,j,k}$  and  $y_{i,j,k}$ , and we drop the last term of Eq. (7) because it is a constant that does not affect the solution of the problem. It is important to highlight that objective function (9a) does not allow for  $y_{i,j,k} = 0$ , even though constraint (8e) does. We will later see that the objective function can be further approximated to allow  $y_{i,j,k} = 0$ .

Since the factors  $w_{j,k}$ ,  $\eta_{i,j,k}$ , and  $h_{i,j,k}$  are positive constants, the optimization problem (9) can be further rewritten as

minimize 
$$\sum_{i,j,k} \exp\left(\alpha_{i,j,k} + \frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln\left(2\right)\right), \quad (10a)$$

subject to Constraints (8b)-(8h), (10b)

where  $\alpha_{i,j,k}$  is a constant defined as

$$\alpha_{i,j,k} \triangleq \ln\left(w_{j,k}\frac{\eta_{i,j,k}}{h_{i,j,k}}\right). \tag{11}$$

We now analyze the convexity of the optimization problem (10). Consider a single term of the summation in the objective function. Any such term is an exponential function whose argument is a linear-fractional function. Since a linearfractional function is quasiconvex, and the exponential function is a non-decreasing function, it follows that each term in the above summation is also quasiconvex. Nevertheless, while convexity is preserved by a non-negative weighted sum operation, quasiconvexity may not be [46]. Therefore, the optimization problem (10) needs to be reformulated before any convex or quasiconvex optimization technique can be applied.

<sup>3</sup>In LTE,  $\theta_{max}$  is approximately 4.8 bits/sec/Hz, based on 64 QAM and 4/5 code rate [45].

(9a)

(8h)

First, since the logarithmic function is a monotonically increasing function, we apply it to the objective function (10a) to create an equivalent optimization problem:

*minimize* 
$$\ln\left(\sum_{i,j,k}\exp\left(\alpha_{i,j,k} + \frac{1}{\beta}\frac{\xi_{i,j,k}r_i}{\rho_{j,k}y_{i,j,k}}\ln\left(2\right)\right)\right),$$
(12a)

Second, we exploit the log-sum-exp approximation

$$\max_{i=1...n} x_i \le \ln \sum_{x=1}^n e^{x_i} \le \max_{i=1...n} x_i + \ln n.$$
(13)

The lower bound is met when there is only one non-zero  $x_i$ ; the upper bound is met when all the  $x_i$  are equal. For a given n, minimizing  $\max_{i=1...n} x_i$  reduces the values of both the upper and lower bounds of  $\ln \sum_{x=1}^{n} e^{x_i}$ . Applying the above approximation to the optimization problem (12), it then becomes

minimize 
$$\max_{i,j,k} \left[ \alpha_{i,j,k} + \frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln\left(2\right) \right], \quad (14a)$$

The objective function (14a) is a maximization of linearfractional functions and, therefore, of quasiconvex functions. Such formulation is also known in the literature as a generalized linear-fractional program. Since a nonnegative weighted maximum of quasiconvex functions is also quasiconvex, so is the above objective function. We can now apply any general approach for quasiconvex programming. One such approach consists in representing the sublevel sets of the quasiconvex function via a family of convex inequalities [46], as we will now describe.

First, we define  $g_0(\xi, y)$  as our current objective function:

$$g_0(\xi, y) = \max_{i,j,k} \left[ \alpha_{i,j,k} + \frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln(2) \right].$$
(15)

Second, for a given parameter  $\mu$ ,  $g_0(\xi, y) \leq \mu$  if and only if

$$\max_{i,j,k} \left[ \xi_{i,j,k} r_i \ln (2) - \beta \rho_{j,k} y_{i,j,k} \left[ \mu - \alpha_{i,j,k} \right] \right] \le 0.$$
 (16)

If we define the convex function  $\vartheta_{\mu}(\xi, y)$  as

$$\vartheta_{\mu}(\xi, y) = \max_{i,j,k} \left[ \xi_{i,j,k} r_{i} \ln \left( 2 \right) - \beta \rho_{j,k} y_{i,j,k} \left[ \mu - \alpha_{i,j,k} \right] \right],$$
(17)

then

S

$$g_0\left(\xi, y\right) \le \mu \Leftrightarrow \vartheta_\mu\left(\xi, y\right) \le 0. \tag{18}$$

Therefore, the  $\mu$ -sublevel set of the quasiconvex function  $g_0$  is the 0-sublevel set of the convex function  $\vartheta_{\mu}$ .

Let us denote the optimal value of the quasiconvex optimization problem (14) as  $\chi^*$ . If the feasibility problem

find 
$$\xi, y,$$
 (19a)

*ubject to* 
$$\vartheta_{\mu}(\xi, y) \le 0,$$
 (19b)

is feasible, then  $\chi^* \leq \mu$  and any feasible point  $(\xi, y)$  is also a feasible point for the quasiconvex problem (14). If the

problem (19) is not feasible, then  $\chi^* > \mu$ . Problem (19) is a convex feasibility problem. Therefore, we can verify whether  $\chi^*$  is greater or less than a particular value  $\mu$  by solving problem (19). Based on this last observation, a simple procedure to find  $\chi^*$ , BIMEM, is designed through a bisection method that solves a convex feasibility problem at every step, as described in Algorithm 1.

Algorithm 1 BIMEM: Bisection method for energy minimization.

1: given  $l_1 \leq \chi^*, l_2 \geq \chi^*, \epsilon > 0$ 2: repeat 3:  $\mu = (l_2 + l_1)/2$ Solve the convex feasibility problem (19) 4: 5: if (19) is feasible then 6:  $l_1 = \mu$ 7: else 8:  $l_2 = \mu$ end if 9: 10: **until**  $l_2 - l_1 \le \epsilon$ 

In Algorithm 1, assuming that the quasiconvex problem (14) is feasible and that we know an interval  $[l_1, l_2]$  that contains the optimal value  $\chi^*$ , we solve the feasibility problem at the midpoint  $\mu = (l_1 + l_2)/2$  of such interval by applying any convex optimization technique, e.g., interior-point method. The result of the feasibility problem indicates whether  $\chi^*$  is in the lower or upper half of the interval, which we then use to update the interval accordingly. The new interval is half the size of the initial one, i.e., it is bisected. This procedure is repeated until the size of the interval satisfies some lower bound  $\epsilon$ . After *m* iterations, the size of the interval before the algorithm terminates is  $\left[\log_2\left((l_2 - l_1)/\epsilon\right)\right]$ .

To apply Algorithm 1, we need the initial interval  $[l_1, l_2]$  that is guaranteed to contain the optimal value  $\chi^*$ . Such interval can be obtained from constraint (19b), as shown below. For such constraint to be satisfied, the following expression must be true:

$$\max_{i,j,k} \left[ \xi_{i,j,k} r_i \ln \left( 2 \right) - \beta \rho_{j,k} y_{i,j,k} \left[ \mu - \alpha_{i,j,k} \right] \right] \le 0,$$
 (20)

which is equivalent to

$$\xi_{i,j,k} r_i \ln(2) - \beta \rho_{j,k} y_{i,j,k} \left[ \mu - \alpha_{i,j,k} \right] \le 0, \quad \forall i, j, k.$$
 (21)

Since  $r_i$  is positive and  $\xi_{i,j,k}$  is non-negative, then the first term is also non-negative. Therefore, we need the second term to be non-positive. As a result, there are two possible necessary conditions for the above expression to be satisfied for any given i,j,k:

$$\mu - \alpha_{i,j,k} \ge 0, \quad \text{or} \tag{22}$$

$$\xi_{i,j,k} = y_{i,j,k} = 0. \tag{23}$$

From Eq. (22) we have that  $\mu \ge \alpha_{i,j,k}$ . Since  $\chi^*$  corresponds to the smallest  $\mu$  for which  $g_0(\xi, y) \le \mu$ , we can now obtain an interval  $[l_1, l_2]$  that is guaranteed to include the optimal

value  $\chi^*$  by finding the minimum and maximum values of  $\alpha_{i,j,k}$ :

$$l_1 = \min_{i,j,k} \alpha_{i,j,k},\tag{24}$$

$$l_2 = \max_{i,j,k} \alpha_{i,j,k}.$$
 (25)

With such interval, we can now apply Algorithm 1 to find the optimal value  $\chi^*$  for the energy minimization problem. Once such value is found, the energy minimization problem can be expressed as a single convex feasibility problem:

find 
$$\xi, y,$$
 (26a)

subject to 
$$\xi_{i,j,k}r_i \ln(2) - \beta \rho_{j,k}y_{i,j,k} [\chi^* - \alpha_{i,j,k}] \leq 0,$$
  
 $\forall i, j, k,$  (26b)

However, the optimum UE-to-CC association policy can be directly obtained from knowing  $\chi^*$  without the need to solve this last optimization problem. From Eq. (22) and Eq. (23), we have that if  $\chi^* \leq \alpha_{i,j,k}$ , then  $\xi_{i,j,k} = y_{i,j,k} = 0$ . By plugging in the definition of  $\alpha_{i,j,k}$  from Eq. (11), we can state in an equivalent way that the optimum UE-to-CC association policy for energy minimization is for UE *i* to associate with  $CC_{j,k}$  if and only if

$$\frac{h_{i,j,k}}{\eta_{i,j,k}} > w_{j,k} e^{-\chi^*}.$$
 (27)

Since we obtained the above solution using the log-sumexp approximation described in Eq. (13), it follows that the approximation gap is  $\ln n$ , where *n* is the product of the number of UEs, the number of layers, and the number of CCs per layer.

# B. Load Balancing for Joint Energy Minimization and Capacity Maximization

In Section III-A, we analyzed the energy minimization problem in a HetNet where MSCA is supported. Even though the operators are able to reduce their economic and environmental impact by minimizing the energy consumption, they are typically interested in finding a balance between reducing the energy consumption and maximizing the network capacity. In this section, we analyze how these two conflicting objectives can be addressed jointly.

In a capacity maximization problem, the objective function generally follows the form of

$$f_1(\xi) = \sum_i r_i U\left(\sum_j \sum_k \xi_{i,j,k}\right), \quad \text{or} \qquad (28)$$

$$f_2(\xi) = \sum_j U\left(\sum_k \sum_i r_i \xi_{i,j,k}\right),\tag{29}$$

where U is a concave function. A typical approach used in the literature is to consider U to be a logarithmic function. In such case,  $f_1(\xi)$  represents a metric of fairness across multiple UEs, i.e., it is better to increase the bit rate of a user that is experiencing a low bit rate than to increase that of a user with an already high bit rate. Similarly,  $f_2(\xi)$  represents a metric of load fairness across BSs, i.e., it is better to increase the total load (bit rate) carried by an underloaded BS than to increase the load of a BS that is already carrying a high load. Rather than focusing on a specific case, we will utilize a generic concave function  $f_3(\xi)$ . For such function, the capacity maximization problem can be expressed as

maximize 
$$f_3(\xi)$$
, (30a)

subject to 
$$\sum_{j} \sum_{k} \xi_{i,j,k} \ge 1, \quad \forall i,$$
 (30b)

$$\sum_{i} y_{i,j,k} \le 1, \qquad \qquad \forall j,k, \qquad (30c)$$

$$\begin{aligned} \xi_{i,j,k} \ge 0, & \forall i, j, k, & (30d) \\ y_{i,j,k} \ge 0, & \forall i, j, k, & (30e) \end{aligned}$$

$$r_i\xi_{i,j,k} - \rho_{j,k}\theta_{\max}y_{i,j,k} \le 0, \quad \forall i, j, k.$$
(30f)

$$\xi_{i,j,k} = 0; \qquad \qquad \forall i, j, k, \operatorname{CC}_{j,k} \notin \Gamma_i$$
(30g)

$$y_{i,j,k} = 0;$$
  $\forall i, j, k, CC_{j,k} \notin \Gamma_i$ 
(30h)

The only difference between the above constraints and the ones of the energy minimization problem is that here, the UE total QoS requirement  $r_i$  no longer needs to be satisfied with equality; rather, it is the lower bound, specified by constraint (30b). Therefore, the domain of the energy minimization problem is a subset of the one of the capacity maximization problem. Moreover, any feasible point for the energy minimization problem (8) is also feasible for the capacity maximization problem (30). Also, note that the inputs required from the UEs to solve the capacity maximization problem (30) are the same as for the energy minimization problem (8).

We can reformulate the capacity maximization problem as a convex minimization problem:

minimize 
$$f_4(\xi) \equiv -f_3(\xi)$$
, (31a)

where  $f_4(\xi)$  represents the new objective function. Since  $f_4$  is the negative of a concave function, it is convex. If we denote by  $f_0(\xi, y)$  the objective function of the energy minimization problem, then the problem of jointly minimizing the energy consumption and maximizing the network capacity can be expressed as

minimize 
$$\begin{bmatrix} f_0(\xi, y) \\ f_4(\xi) \end{bmatrix}$$
, (32a)

i.e., as a *multi-criterion* or *multi-objective* optimization problem. It is important to note that  $f_0$  and  $f_4$  are competing functions, i.e., one of them is minimized at the expense of increasing the other. Because of this competing nature, no single point is capable of jointly achieving the minimum value that  $f_0$  and  $f_4$  could achieve separately. However, since a multi-objective optimization is a vector optimization defined over a cone  $K = \mathbb{R}^m_+$  for some m > 0, we can scalarize the problem to find Pareto-optimal points for the original problem.

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Applying scalarization to the optimization problem (32), we obtain

problem (36) is equivalent to a single convex feasibility problem

minimize 
$$v f_0(\xi, y) + (1 - v) f_4(\xi)$$
, (33a)

where  $0 \le v \le 1$  is a parameter that is adjusted to find the Pareto-optimal points. Intuitively, v is selected to indicate the operator's balance point between the energy minimization and the capacity maximization. For v close to 1, a greater weight is given to the energy minimization. Conversely, for v close to 0, a greater weight is given to the capacity maximization.

In general, for a given v, if  $f_0$  and  $f_4$  are convex functions, then the scalarized optimization problem is a convex one. We have shown that  $f_4$  is a convex function, and, in Section III-A, we found that the energy minimization problem can be expressed as the convex feasibility problem (26). The issue with using the objective function of the latter is that, by definition, the objective function of a feasibility problem is a constant independent of the optimization variables. If we were to consider  $f_0$  a constant, then it would have no effect on the solution of the optimization problem (33), i.e., such optimization problem would be reduced to the capacity maximization problem. Therefore,  $f_0$  cannot be directly taken from the convex feasibility problem (26). However, we can obtain an appropriate  $f_0$  from the original formulation of energy minimization problem, as we will now describe.

If we apply the weight factor v to the objective function of the original formulation of the energy minimization problem in (8), such problem becomes

minimize 
$$v \sum_{j} \sum_{k} \hat{P}_{\text{on,dyn}}(\text{CC}_{j,k}),$$
 (34a)

which, after similar transformations as the one followed during the analysis of the energy minimization problem, becomes equivalent to

minimize 
$$\ln\left(\sum_{i,j,k}\exp\left(\ln\left(v\right)+\frac{\xi_{i,j,k}r_{i}\ln\left(2\right)}{\beta\rho_{j,k}y_{i,j,k}}+\alpha_{i,j,k}\right)\right)$$

subject to Constraints (8b)-(8h). (35b)

Applying the log-sum-exp approximation described in Section III-A, the above optimization problem can be approximated as

*minimize* 
$$\max_{i,j,k} \left[ \ln(\upsilon) + \alpha_{i,j,k} + \frac{1}{\beta} \frac{\xi_{i,j,k} r_i}{\rho_{j,k} y_{i,j,k}} \ln(2) \right],$$
(36a)
*subject to* Constraints (8b)-(8h).
(36b)

For v = 1, the above problem is reduced to the original energy minimization problem. Therefore, for v = 1 and following a similar development as in Section III-A, the optimization

ind 
$$\xi, y,$$
 (37a)

subject to 
$$\xi_{i,j,k}r_i \ln (2) - \beta \rho_{j,k}y_{i,j,k} [(\chi^* - \ln (\upsilon)) - \alpha_{i,j,k}] \leq 0, \quad \forall i, j, k, \quad (37b)$$
  
Constraints (8b)-(8h).  $(37c)$ 

If we consider 0 < v < 1 in the above problem, we note that its impact translates into increasing the effective threshold  $(\chi^* - \ln(v))$  of the optimization problem, since  $\ln(v) < 0$ . More importantly, in the above feasibility problem, the factor v is part of the constraint rather than of the objective function. Therefore, the problem above does not suffer from v not impacting the optimization problem (33), as was the case when we directly used problem (30). So, combining the objective function and constraints of the above problem with that of the capacity maximization as per the formulation of problem (33), we obtain that the scalarized multi-objective optimization becomes

$$minimize \quad -f_3\left(\xi\right), \tag{38a}$$

subject to 
$$\xi_{i,j,k}r_i \ln(2) - \beta \rho_{j,k}y_{i,j,k} \left[ \left( \chi^* - \ln(\upsilon) \right) \right]$$

$$-\alpha_{i,j,k}] \le 0, \qquad \forall i, j, k, \tag{38b}$$

From the above problem formulation, we can also directly obtain the optimum UE-to-CC association policy without the need to find the solution. As in the case of the energy minimization problem, there are two possible necessary conditions for constraint (38b) to be satisfied:

$$(\chi^* - \ln(\upsilon)) - \alpha_{i,j,k} > 0, \quad \text{or}$$
 (39)

$$\xi_{i,j,k} = y_{i,j,k} = 0. \tag{40}$$

Therefore, if  $(\chi^* - \ln(v)) \leq \alpha_{i,j,k}$ , then  $\xi_{i,j,k} = y_{i,j,k} = 0$ . By plugging in the definition of  $\alpha_{i,j,k}$  from Eq. (11), we can state in an equivalent way that the optimum UE-to-CC association policy for any given v in the multi-objective optimization of energy minimization and capacity maximization is for UE *i* to associate with  $CC_{j,k}$  if and only if

$$\frac{h_{i,j,k}}{\eta_{i,j,k}} > w_{j,k} \exp\left(-\left(\chi^* - \ln\left(\upsilon\right)\right)\right).$$
(41)

Once the UEs associate with the CCs, the values of the optimization variables  $\xi$  and y will depend on the particular function  $f_3$  utilized as objective function of the capacity maximization problem. It is important to note that, to perform the multi-objective optimization, we need to find the value of  $\chi^*$  only once, and then the UE-to-CC association policy is defined by that value, the operator-defined v, and the specific capacity maximization function of interest.

## **IV. PERFORMANCE EVALUATION**

In this section, we evaluate the performance of our proposed algorithms for MSCA-enabled HetNets to minimize the energy consumption and balance it with the capacity maximization. The simulation parameters are shown in Table I. We have This article has been accepted for publication in a future issue of this journal, but has not been fully edited. Content may change prior to final publication. Citation information: DOI 10.1109/TWC.2016.2602336, IEEE Transactions on Wireless Communications

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 TABLE I

 Simulation parameters for multi-layer HetNets with MSCA.

Parameter	Value
CC per BS (per layer)	[1,1,1] CC
Bandwidth of a CC (per layer)	[20, 10, 2.5] MHz
Number of antennas at BS	1
Max. spectral efficiency ( $\theta_{max}$ )	4.8 bps/Hz
Total coverage area	1km x 1km
β	0.75
Number of active UEs	50
Altitude of UEs	1.5 m
Number of antennas at UE	1
Number of layers	3
Type of BSs (per layer)	[macro,pico,pico]
Number of BSs (per layer)	[1,5,15]
Altitude of BSs (per layer)	[25,20,10]m
Power weight of a CC (per layer)	[2.66,3.1,4.0]

chosen to assign only one CC to every BS in every layer so that our results capture the effects of MSCA rather than those of the classical CA. Based on the bandwidth parameters, we have that layer 1 (L1), layer 2 (L2), and layer 3 (L3) provide 18.6%, 46.51%, and 34.88% of the network capacity, respectively. Thus, L1 is meant to provide basic coverage, L2 is meant to provide basic capacity, and L3 is meant to enhance the capacity. BSs per layer and active UEs are uniformly distributed across the total coverage area.

For the path loss, we use the following 3GPP models for heterogeneous networks in outdoor scenarios (distance D (in km)) [47]:

$$(macro)PL = 128.1 + 37.6\log(D),$$
 (42)

$$(pico)PL = 140.7 + 36.7log(D).$$
 (43)

To evaluate the overall performance of the energy-saving algorithm, we applied it to 100 different scenarios generated using the parameters from Table I. For each scenario, Algorithm 1 was evaluated for a minimum QoS varying in the range [1, 10]Mbps. To solve the convex feasibility problem in step 4 of Algorithm 1, we utilized CVX [48] [49], a Matlabbased modeling system for convex optimization, together with MOSEK [50], one of the leading commercial software products for large-scale optimization problems. In 91% of the 1000 scenario-QoS combinations and a lower bound  $\epsilon = 0.01$ , our algorithm required 11 iterations to converge to a solution and 12 iterations in the rest of the cases. This result highlights the high convergence rate achieved by the initial estimation of the interval  $[l_1, l_2]$  from Eq. (24) and Eq. (25).

Figure 2 depicts the percent of UEs using MSCA and the mean UE spectral efficiency. From this figure, we observe that the percent of UEs using MSCA increases from less than 5% to nearly 35% as the minimum QoS requirement increases from 1 to 10Mbps. For this same variation of the minimum QoS requirement, the mean UE spectral efficiency grows from nearly 2.5bps/Hz to 4.7bps/Hz, i.e., it almost reaches the maximum spectral efficiency of 4.8bps/Hz.

The fact that most UEs are operating at nearly maximum spectral efficiency prevents more UEs from applying MSCA since such event would require a first set of UEs to empty part of its currently allocated spectrum so that a second set of



Fig. 2. Percent of UEs using MSCA and mean UE spectral efficiency.

UEs, currently connected to other layers, can utilize the freed spectrum. However, such release of spectrum would imply that the UEs of the first set have to further increase their own spectral efficiency.

Figure 3 shows several per-layer metrics. In Figure 3a, we depict how the UEs associate with each BS layer. Here, we observe that as the minimum QoS requirement increases, the percent of UEs associated with L1 and L3 experiences small variations, indicating that most UEs remain connected to those layers. However, the percent of UEs attached to L2, the layer with highest capacity, increases significantly, indicating that most UEs are applying MSCA by connecting to an additional CC in L2. In Figure 3b, we observe that as the minimum QoS requirement increases, the percent of the load carried by L3 decreases from 51% to 34% while that of L2 increases from 24% to 47%. From Figure 3c, we observe that the change in the load managed by L2 and L3 produces a nearly equivalent change in the percent of energy consumption. That of L3 decreases from 30% to 19% while that of L2 increases from 35% to 56%.

An additional metric of interest is the value of  $\chi^*$  as the minimum QoS requirement increases. This behavior is depicted in Figure 4. When the minimum QoS requirement is less than 7Mbps,  $\chi^*$  increases almost linearly from -1.4 to 0.05. However, beyond 7Mbps,  $\chi^*$  increases rapidly until reaching a value of 2.44.

To quantify the amount of energy savings provided by our energy-saving algorithm, as well as to characterize the energycapacity trade-off in an MSCA-enabled HetNet, we take a single instance of a HetNet generated with the parameters of Table I, and analyze its performance as the factor v varies from 0 to 1, representing a shift from the capacity maximization to the energy minimization objective. We analyze the balance of energy minimization against three objective functions for the capacity maximization: classical capacity maximization  $(f_{3,1})$ , global UE fairness  $(f_{3,2})$ , and per-BS UE fairness  $(f_{3,3})$ . Their respective definitions are as follows:

$$f_{3,1}(\xi) = \sum_{i} \sum_{j} \sum_{k} r_i \xi_{i,j,k},$$
(44)



Fig. 3. Users, load, and energy per layer.



Fig. 4.  $\chi^*$  vs. minimum QoS requirement.



Fig. 5. MSCA UEs in the energy-capacity optimization.

$$f_{3,2}(\xi) = \sum_{i} \log\left(\sum_{j} \sum_{k} r_i \xi_{i,j,k}\right),\tag{45}$$

$$f_{3,3}(\xi) = \sum_{j} \sum_{i} \log\left(\sum_{k} r_i \xi_{i,j,k}\right).$$
(46)

In Figure 5, we show the percent of UEs that use MSCA. For the classical capacity maximization objective, we observe that very few UEs apply MSCA regardless of the value of v. This behavior occurs because such objective tends to favor UEto-CC links with higher SINR; therefore, MSCA links with distant BSs tend to be disregarded. On the other extreme, we have the per-BS UE fairness. In this case, the number of UEs applying MSCA is over 90%. This behavior occurs because each BS tries to provide a fair amount of throughput to all the UEs that it can potentially serve; therefore, this objective function encourages the application of MSCA among all the UEs that are under the coverage of more than one layer. We observe that the global UE fairness, with the use of MSCA decreasing from 64% to 30% as v varies from 0 to 1, falls roughly in the middle between the other two extremes capacity and per-BS UE fairness. These three graphs suggest that reconfiguring the balance between energy minimization and capacity maximization, i.e., changing the value of v, will have the greatest impact on the UE-to-CC association when the objective function is that of Global UE Fairness. Thus, the network stability would require more attention in such reconfiguration scenario than when the other objective functions are used.

In Figure 6, we depict the capacity usage and the energy consumption. From Figure 6a, we observe that by applying the energy minimization algorithm it is possible to decrease the energy consumption to at least 15% of its maximum for all the capacity objectives. The effect of v on the network capacity usage is shown in Figure 6b. From this graph, we observe that minimizing the energy consumption has the greatest impact, from 90% to 68%, on the capacity usage for the per-BS UE fairness objective. Conversely, the classical capacity objective experiences the least impact, from 99% to 91.45%. In Figures 6a and 6b, it is important to notice that the greatest



Fig. 6. Energy consumption and capacity usage in the energy-capacity optimization.

changes in energy consumption and energy capacity usage occur as the value of v increases from zero to approximately 0.4; nonetheless, in such interval the rate at which the energy consumption decreases is faster than that at which the capacity usage decreases. This suggests that a good trade-off between both objectives can be achieved.

From the above graphs, we can now generate the energycapacity trade-off curve for the MSCA-enabled HetNet, as shown in Figure 7. From this graph, we observe that indeed a good trade-off is achievable between both objectives: reducing the capacity usage by as little as 5% allows to significantly increase the energy savings in all of the three capacity objectives. However, even though it is possible to augment the energy savings by further reducing the capacity usage, the return from such reduction tends to diminish, particularly for the per-BS UE fairness objective.

# V. CONCLUSIONS

MSCA has been introduced as a mechanism to increase the amount of bandwidth available to the users for HetNets in 5G cellular systems. However, existing work has focused on



Fig. 7. Trade-off curve for the energy savings vs. capacity usage.

exploiting the use of MSCA to maximize the network capacity, disregarding the energy efficiency of MSCA. In this paper, we studied the problem of minimizing the energy consumption in MSCA-enabled HetNets and developed an efficient algorithm to solve it. We showed that, by utilizing a quasiconvex relaxation, we are able to not only solve the problem, but also to establish a clear and simple cell-association policy. Moreover, we showed how this cell-association policy can be easily adjusted to obtain a new policy that balances the conflicting objectives of energy minimization and capacity maximization. Through extensive simulations, we characterized the effects of our algorithm on the percent of load, users, and energy per layer, as well as on the percent of UEs that use MSCA and their average spectral efficiency. In addition, we obtained the trade-off curve between the energy minimization and capacity maximization and found that a large amount of energy savings can be achieved in an MSCA-enabled HetNet by reducing the network capacity usage by as little as 5%.

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